GRASSMIND 2.0 – grassland model

1 Overview and general concept

The grassland model GRASSMIND is designed to simulate grasslands and combines biogeochemical cycles with biodiversity (Taubert et al. 2012). The model includes additional submodels that allow for analyzing plant-soil feedbacks and effects of management and climate change. A first conceptual model description (GRASSMIND 1.0) has been described earlier (Taubert et al. 2012). Since then, progress in the model development has been made in terms of modeling the nitrogen demand of plants and nitrogen relocation, as well as the coupling with soil models.

GRASSMIND 2.0 is an individual-based and process-oriented model that follows the gap approach typically applied in forest models (Fischer et al. 2016, Botkin et al. 1972, Köhler & Huth 2004, Shugart 1998). Grassland is simulated on an area of size $A$ (m$^2$), which is a composite of regularly ordered patches of $a = 1$ m x 1 m in size and described by their location within the area $A$ (Fig. 1). Individual plants interact and compete for resources on one patch without assignment of explicit spatial locations to each plant (Fig. 1). Intra- and interspecific competition for resources and their resulting uptake influence the productivity of plants. Aboveground resources include light and space and belowground resources comprise soil water and nitrogen.

For simulating soil resource dynamics, GRASSMIND is coupled with two soil models: (i) CANDY (Franko et al. 1995) and (ii) CENTURY (Parton et al. 1988).

Biogeochemical cycles include the carbon, nitrogen and water fluxes in the grassland ecosystem. The growth of single plants is modeled based on a carbon balance of gross primary production (GPP) and respiration. Adding leaf and root turnover and demographic process (like seed ingrowth and plant mortality), the carbon cycle is extended to the plant community and is closed via litter decomposition and soil carbon processes for the grassland ecosystem. The nitrogen cycle is modeled in close connection to the carbon cycle by assuming CN ratios for plants (green and senescent leaves and roots) and soil pools. The water cycle includes as main processes interception, evaporation, water infiltration and percolation in soil as well as plant transpiration.

Biodiversity is integrated in the model by either simulating single species or plant functional types (aggregated species with similar functional behavior; PFT). Species
or PFT can differ in traits which determine their demographic rates, growth and behavior in competition with other plants. Plants of the same species or PFT do not differ in their traits, but can have different ages or sizes. The geometry of an individual plant is described by the aboveground shoot (here, leaves) and belowground root system (root branches).

The processes included in the grassland model are modeled according to a specific schedule (Fig. 1):

(A) recruitment and emergence of plant seedlings (1,2)
(B) plant senescence and mortality (3-5)
(C) gross production (incl. shading and competition for soil water and nitrogen, 6-10,13)
(D) plant respiration (for maintenance and growth, 11)
(E) net production and allocation for plant growth (12,14)
(F) management (15)

The grassland model runs at daily time steps (Δt = 1). For the purpose of shading and crowding mortality, the aboveground space is discretized into vertical height layers of constant width Δh (Tab. 1).

Table 1. Overview of general input parameter for GRASSMIND.

<table>
<thead>
<tr>
<th>Description</th>
<th>Parameter</th>
<th>Unit</th>
<th>Value</th>
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<tbody>
<tr>
<td>Time step</td>
<td>Δt</td>
<td>d</td>
<td>1</td>
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<tr>
<td>Simulation area</td>
<td>A</td>
<td>m²</td>
<td>1 ... 100</td>
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<tr>
<td>Patch area</td>
<td>a</td>
<td>m²</td>
<td>1</td>
</tr>
<tr>
<td>Width of height layers</td>
<td>Δh</td>
<td>m</td>
<td>0.01</td>
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</tbody>
</table>
Figure 1: Overview of main processes in GRASSMIND.

Numbers in brackets within each box show the serial order of their calculation within one time step $\Delta t$. Grey frames that underlie these boxes group them according to the main processes and their corresponding chapters. Rhombuses indicate climatic input parameters with the following abbreviations: $PET$ – potential evapotranspiration, $PPFD$ – photoactive photon flux density. Spatial scale of a process is marked by different colors (green = patch, yellow = individual plant).

2 The geometry of an individual

Each individual plant is characterized by the following state variables (organic dry matter in g$_{ODM}$):

(1) aboveground shoot biomass $B_{shoot}$
(2) belowground root biomass $B_{root}$
(3) reproduction biomass $B_{rep}$

The aboveground shoot biomass is divided into biomass of fresh green leaves $B_{shoot}^{green}$ and biomass of senescent yellow leaves $B_{shoot}^{sen}$. Further state variables, which describe the geometry of an individual, can be derived from allometric relationships with species-specific attributes (Fig. 2).
Figure 2: Geometry of a single plant in GRASSMIND. State variables that correspond with the geometrical characteristics of an individual plant and that can be derived from the aboveground shoot and belowground root biomass.

2.1 The aboveground shoot
We model the aboveground shoot of an individual plant encased by a cylinder. The volume of the encasing cylinder $V_{cylinder}$ [m$^3$] is related to the shoot biomass:

$$V_{cylinder} = \frac{B_{shoot}}{f_s}$$

where the species-specific correction factor $f_s$ [g$\text{OM}$/m$^3$] accounts for free space within the cylinder not filled with biomass. A species-specific constant parameter $hw$ defines the ratio between plant height $h$ [m] and width $w$ [m] of the assumed cylinder.

The space an individual plant occupies on a patch is determined by the ground area $cov$ [m$^2$] of the encasing cylinder. To calculate a patch's vegetation cover $CC$ (the area occupied by all individuals relative to the patch area), it is necessary to take leaf overtopping or overlapping among individual plants into account. For this, each plant cover is corrected by a species-specific overlapping factor $f_o$ (unitless). This factor accounts for overlapping in an implicit manner since the individuals do not have spatially explicit positions within the patch. The corrected covers of all plants on the patch are summed up and normalized by the patch area:
\[ CC = \frac{1}{a} \cdot \sum_{all\ individuals} (cov \cdot f_o) \]  

(2)

The leaf area of the aboveground shoot is obtained by multiplying the plant’s biomass \( B_{shoot} \) with the constant parameter of specific leaf area \( SLA \) [m²/g ODM]. This includes the assumption that all leaves have the same \( SLA \), leading to the overall plant leaf area index \( L \) [m²/m²]:

\[ L = \frac{B_{shoot} \cdot SLA}{cov} \]  

(3)

By using only the green shoot biomass \( B_{shoot}^{green} \) instead of \( B_{shoot} \) in equation (3), we obtain the green leaf area index \( L_{green} \) which is especially important for photosynthesis (see section 3.5).

### 2.2 The belowground root

We assume a species-specific allometric relationship between an individual’s aboveground shoot biomass \( B_{shoot} \) and belowground root biomass \( B_{root} \) – determined by the parameters \( sr \) (defining the species-specific shoot-root ratio of a plant in terms of biomass):

\[ B_{shoot} = sr \cdot B_{root} \]  

(4)

The individual’s ability to access and compete for soil nitrogen and water resources strongly depends on its root system. In addition to root biomass, the root system’s vertical distribution in soil is also considered. Shallow and highly branched root systems are beneficial for nutrient uptake as most nutrients occur predominantly in the upper soil layers. In contrast, deeper root systems strongly increase the individual’s access to soil water resources, particularly during drought periods.

To calculate the rooting depth \( depth_{root} \) [m], which is required for water uptake, we adapt the power-law approach (Schenk & Jackson 2002) which functionally relates rooting depths to the aboveground ellipsoidal canopy volume. Using the same relationship for the volume of an individual’s aboveground shoot cylinder (equation 1) and including the shoot-root ratio (equation 4) leads to:

\[ depth_{root} = r_1 \cdot \left( \frac{sr}{f_s} \cdot B_{root} \right)^{r_2} \]  

(5)
where the species-specific parameters $r_1$ and $r_2$ define the dependence of the rooting depth on plant biomass. Each individual has its own rooting system, irrespective of whether the individual plant has been recruited via generative or vegetative reproduction. The total branching root length $length_{\text{root}}$ [m], which is important for nitrogen uptake, is related to root biomass via the species-specific parameter specific root length $SRL$ [m/gODM]:

$$length_{\text{root}} = B_{\text{root}} \cdot SRL$$  (6)

3 Model processes

In the following, we describe the details of the modeled processes important within the life cycle of an individual plant. These have already been introduced in brief (see chapter 1, Fig. 1).

3.1 Recruitment

3.1.1 Reproduction

We distinguish three different sources of species-specific recruitment of plants:

- seed rain from a surrounding meta-community
- local reproduction of plants
- sowing of seeds

Seed rain from a surrounding meta-community is modeled by a constant species-specific seed input rate $N_{seed}^{\text{meta}}$ (in [1/m²/d], starting pre-defined at $t_{\text{meta}}$) while sowing throws $N_{seed}^{\text{sow}}$ seeds (in [1/m²]) to the patch only at time $t_{\text{sow}}$.

In contrast, local recruitment by mother plants is dependent on their fitness. In its current version, GRASSMIND does not explicitly distinguish between vegetative and generative reproduction. Here, we assume that the single seed biomass produced via generative reproduction equals the biomass investment also required for vegetative reproduction (e.g. rhizomes or stolones). The number of locally recruited seedlings $N_{seed}^{\text{local}}$ (in [1/m²/d]) produced by a reproductive mother plant is dependent on the mother plant’s net production $NPP$ allocated to its reproduction pool $B_{\text{rep}}$ (see section 3.13) and the species-specific seed biomass $B_{seed}$ [gODM]:


\[ N_{seed}^{local} = \frac{B_{rep}}{B_{seed}} \]

The total number of potentially germinating seeds \( N_{seed} \) \([1/m^2/d]\) is then determined by:

\[ N_{seed} = N_{seed}^{meta} + N_{seed}^{sow} + N_{seed}^{local} \]  

(8)

### 3.1.2 Emergence of new seedlings

Only a limited number \( \hat{N}_{seed} \) of potential seedlings can germinate successfully within the same patch:

\[ \hat{N}_{seed} = N_{seed} \cdot germ_{\%} \]  

(9)

where \( germ_{\%} \) denotes the germination rate (unitless). In the current version of GRASSMIND, environmental conditions are not explicitly considered for the germination process, so the germination rate can be interpreted as a constant species-specific success rate.

The successfully germinated seedlings emerge dependent on an emergence time \( t_{em} \) [d] since seed rain and have an initial height \( h_{min} \) [m] (further geometrical properties can be derived from \( h_{min} \)).

At the time of emergence, seeds could additionally fail to establish in terms of limited space. If the emergence of all potentially germinating seeds would increase total vegetation cover \( CC \) above a patch’s area (i.e. > 100\%), only those seeds (for each species) proportional to the remaining free space on the patch will establish successfully (see also section 3.3.3). All seeds that failed to emerge are directly transferred to the litter pool.

### 3.3 Mortality

#### 3.3.1 Senescence of leaves and root branches

All plants are subject to tissue turnover as a result of partial yellowing of leaves and the death of root branches. The transfer rate from green to yellow (senescent) shoot biomass \( B_{sen}^{shoot} \) is defined by the reciprocal value of the leaf life span \( LLS \) [d].
Senescent shoot leaves remain attached to an individual’s shoot geometry and thus can still shade other leaves, but do not photosynthesize any longer. The transfer of senescent shoot biomass into the surface litter pool occurs either (a) if an entire plant dies or (b) at the turn of the year.

Equivalent to leaf senescence, the transfer rate of root branches into dead root biomass is defined by the reciprocal value of the root life span $RLS\ [d]$. Dead root parts do not remain within an individual’s root system and geometry and are immediately transferred to the soil litter pool.

### 3.3.2 Base mortality

A base mortality is modeled using a daily constant rate $m_b\ [1/d]$. The value of this rate is a pre-defined parameter and allows differentiating dependent on the individual plant age (e.g. seedlings versus mature plants):

$$m_b = \begin{cases} 
0 &, \text{age} = 0 \\
\frac{m_{\text{seed}}}{\text{age} - \text{age}_{\text{rep}}} &, 0 < \text{age} < \text{age}_{\text{rep}} \\
\frac{m_{\text{basic}}}{\text{age}_{\text{rep}} - \text{age}} &, \text{age}_{\text{rep}} \leq \text{age} < \text{life} \\
1 &, \text{age} \geq \text{life}
\end{cases} \quad (10)$$

A basic mortality rate $m_{\text{basic}}$ is used for mature plants, whereas a special mortality rate $m_{\text{seed}}$ is used for seedlings. Plants enter the mature plant state as soon as they start to reproduce (determined by the parameter $\text{age}_{\text{rep}}$). Based on the species-specific lifespan $\text{life}\ [\text{yr}]$ and current age of plants, the rate $m_b$ can be set to one (meaning that plants immediately die). For annual species thus $m_b$ equals one, if the $\text{age}\ [\text{yr}]$ of an annual plant exceeds one year. For bi-annuals and perennials $m_b$ is set to two years or larger, respectively. Dying plants are directly transferred to the litter pool (i.e. to surface and soil litter pools for decomposition).

### 3.3.3 Crowding mortality

Due to space limitations only a finite number of plants are able to survive on a patch. There are different possibilities to define an indicator of limited space at which crowding mortality can be triggered.

Here, we chose an indicator $M_C$ which is defined by the reciprocal of vegetation cover $CC$ on a patch:
If vegetation cover $CC$ exceeds a patch’s area, the indicator $MC$ drops below one. Note that vegetation cover also includes species-specific overlapping factors $f_O$.

Crowding mortality occurs earliest in the subsequent time step. If space is limited ($MC < 1$), a specific number of plants $N_{\text{crowd}} [1/d]$ die stochastically (without any species- or size-specific advantages) so that the factor $MC$ exceeds the threshold of one again:

$$N_{\text{crowd}} = N \cdot (1 - MC)$$  \hspace{1cm} (12)

Dying plants are directly transferred to the litter pool (i.e. to surface and soil litter pools for decomposition).

### 3.4 Light intensity

An increasing number of plants on a patch (which can differ in their plant height) results in shading among the individuals. Therefore, the global radiation $I_0 [\mu \text{mol photons}/\text{m}^2/\text{s}]$ on top of the highest individual is increasingly attenuated down to the bottom of the patch. To calculate vertical light conditions on a patch, the aboveground space is divided into horizontal layers of constant width $\Delta h [\text{m}]$. For each individual, its height $h [\text{m}]$ determines the highest layer $l_{\text{max}}$ which is covered by its shoot:

$$l_{\text{max}} = \left\lfloor \frac{h}{\Delta h} \right\rfloor$$  \hspace{1cm} (13)

Since the leaf area $L$ is assumed to be uniformly distributed in vertical direction within an individual’s encasing cylinder, the plant’s contribution of leaf area index $\hat{L}_i [\text{m}^2/\text{m}^2]$ is also assumed to be uniformly distributed among the height layers $i=1, \ldots, l_{\text{max}}$:

$$\hat{L}_i = \begin{cases} 
\frac{L \cdot \text{cov}}{h} \cdot \Delta h, & 0 \leq i \leq l_{\text{max}} \\
0, & i > l_{\text{max}}
\end{cases}$$ \hspace{1cm} (14)

where $\text{cov}$ is the ground area of the individual’s encasing shoot cylinder. Summing up these leaf area contributions for all individuals on a patch results in the patch-based community leaf area index $LAI [\text{m}^2/\text{m}^2]$ for each height layer $i$.
where \( k \) denotes the species-specific light extinction coefficient and \( a \) is the area size of the patch. The light extinction coefficient is a species-specific constant parameter and includes the assumption of similar leaf angles of an individual’s shoot.

To determine the irradiance \( I_S \) [\( \mu \text{mol photon/m}^2/\text{s} \)] at the top of an individual, the patch-based leaf area indices \( LAI_i \) of all height layers above the plant’s height are summed up. Light attenuation through these height layers is then calculated using the approach of Monsi and Saeki (1953):

\[
I_S = I_0 \cdot e^{-(\sum_{i > l_{\text{max}}} LAI_i)}
\]

where \( I_0 \) [\( \mu \text{mol photon/m}^2/\text{s} \)] is the incoming photosynthetic photon flux density (PPFD) above canopy modeled as a daily average from sunrise to sunset.

By the calculation of the light climate within grasslands, competition for light between individuals is considered. Species that grow higher receive more light but also affect the light which is received by smaller plants via shading (Fig. 3). Note that not only green but also standing senescent shoot leaves contribute to shading. To reduce the effect of shading (compared to competition between plants for belowground resources) we weight the patch-based leaf area indices \( LAI_i \) each by a factor (here 1/9, which equals a subdivision of a 1 m\(^2\) patch into 9 sub-patches of homogeneous leaf area distribution). Self-shading within a single plant is included at a later stage (equation 19 and 20).
Figure 3: Light competition between individual species of different plant heights. Aboveground space is divided into height layers of width $\Delta h$. Each plant’s leaf area is uniformly distributed among the respective covered height layers. The height layers marked in grey are shaded by plant A and B. Here, plant B is higher than plant A (vertical black arrows) and receives the unreduced incoming irradiance $I_0$. Plant A is shaded by those parts of plant B’s leaf area that are higher than A, and hence receive the reduced irradiance $I_S$ (equation 16).

3.5 Gross primary production

Gross biomass production of a plant is modeled via photosynthesis. Following the approach of Thornley and Johnson (1990), we calculate the gross photosynthetic rate for a single leaf using a saturation function:

$$P_{\text{leaf}} = \frac{\alpha I_{\text{leaf}} P_{\text{max}}}{\alpha I_{\text{leaf}} + P_{\text{max}}}$$

Here, $\alpha$ is the species-specific initial slope of the light response curve [$\mu\text{mol CO}_2/\mu\text{mol photon}$], $P_{\text{max}}$ is the species-specific maximum gross photosynthetic rate [$\mu\text{mol CO}_2/\text{m}^2/\text{s}$], and $I_{\text{leaf}}$ is the incoming irradiance on the leaf surface [$\mu\text{mol photon/ m}^2/\text{s}$]. The latter is derived by correcting the incoming irradiance $I_S$ at the top of an individual:

$$I_{\text{leaf}} = \frac{k}{1-m} \cdot I_S$$

where $k$ is the species-specific light extinction coefficient and $m$ the transmission coefficient. To obtain the gross photosynthetic rate $P_{\text{shoot}}$ [$\mu\text{mol CO}_2/\text{m}^2/\text{s}$] of an entire
plant, the single-leaf photosynthesis (equation 17) is integrated over the individual’s green leaf area index $L_{green}$:

$$P_{shoot} = \int_0^{L_{green}} P_{leaf}(\bar{L}) d\bar{L}$$  \hspace{1cm} (19)$$

leading to:

$$P_{shoot}(l_{leaf}) = \frac{p_{max}}{k} \cdot \ln \left( \frac{\alpha \cdot k \cdot l_{leaf} + p_{max} \cdot (1-m)}{\alpha \cdot k \cdot l_{leaf} \cdot e^{-k \cdot L_{green}} + p_{max} \cdot (1-m)} \right)$$  \hspace{1cm} (20)$$

Multiplying the gross photosynthetic rate (equation 20) by three conversion factors leads to the potential gross primary production $GPP_{pot} \, [g_{ODM}/d]$ of a plant:

$$GPP_{pot} = P_{shoot}(l_{leaf}) \cdot \phi_{ODM} \cdot \phi_{day} \cdot \phi_a$$  \hspace{1cm} (21)$$

where $\phi_{ODM} = 0.63 \cdot 44 \cdot 10^{-6} \, [g_{ODM}/\mu mol CO_2], \hspace{0.2cm} \phi_{day} = 60 \cdot 60 \cdot length_{day} \, [s/d]$ with $length_{day}$ as the number of hours per day from sunrise to sunset, and $\phi_a = cov \, [m^2]$.

### 3.7 Temperature effects

Photosynthesis and respiration are sensitive to temperature changes (Larcher 1976). Gross primary production (equation 21) is reduced for air temperatures $T \, [°C]$ below a threshold of 10 °C according to Schippers and Kropff (2001, see also Larcher 1976, Fig. 4A):

$$R_T = \begin{cases} 
0 & , T \leq -5°C \\
0.02857 \cdot T + 0.142 & , -5°C < T \leq 2°C \\
0.1 \cdot T & , 2°C < T \leq 10°C \\
1 & , 10°C < T 
\end{cases}$$  \hspace{1cm} (22)$$

Maintenance respiration $r_m$ increases with air temperature according to Schippers and Kropff (2001, see also Larcher 1976, Fig. 4B):

$$f_T = \begin{cases} 
0 & , T \leq 0°C \\
0.033 \cdot T & , 0°C < T \leq 15°C \\
\frac{T-25}{10} & , 15°C < T 
\end{cases}$$  \hspace{1cm} (23)$$
3.8 Water competition

The individual’s uptake of water resources from soil is modeled taking into account its demand on the one hand and the soil water available on the other hand. The individual’s water demand $\theta_{\text{demand}}$ [l/d], which is equal to its potential transpiration, is modeled using the water use efficiency concept:

$$\theta_{\text{demand}} = \frac{R_T \cdot \text{GPP}_{\text{pot}}}{\text{WUE}}$$

(24)

where $\text{GPP}_{\text{pot}}$ [gODM/d] is the gross primary productivity, $R_T$ (unitless) is the effect of air temperature on GPP and WUE [gODM/kgH2O] denotes the water use efficiency (assuming 1 kgH2O = 1 lH2O).

We calculate how much soil water resources are available for an individual plant although competing with other plants on a patch. By coupling GRASSMIND with soil models, the soil is divided into layers of constant width $\Delta s$ for which information on soil water resources are provided. Using this vertical soil discretization, we calculate for each plant its rooting zone described by the soil layer $s_{\text{max}}$ [m] (dependent on its current rooting depth):

$$s_{\text{max}} = \left\lfloor \frac{\text{depth}_{\text{root}}}{\Delta s} \right\rfloor$$

(25)

The rooting zone represents the composition of the respective soil layers $j=1,\ldots,s_{\text{max}}$ in which the individual plant is rooting (Fig. 5). To determine the amount of available soil water for the individual plant, we calculate the soil water content $\theta_{W}^{\text{plant}}$ [V%],
permanent wilting point $\theta_{\text{PWP}}^{\text{plant}}$ [V%] and field capacity $\theta_{\text{FC}}^{\text{plant}}$ [V%] of the plant’s rooting zone by summing up these variables for all layers in the rooting zone.

Figure 5: Illustration of the rooting zones of two different individuals. Horizontal dark grey shadow marking the first three soil layers indicates the rooting zone of individual A. In this example, the rooting zone of individual B covers nearly the entire soil.

Water demand which can actually be fulfilled is determined by:

$$ R_W = \begin{cases} 0, & \theta_W^{\text{plant}} < \theta_{\text{PWP}}^{\text{plant}} \\ \frac{\theta_{\text{W}}^{\text{plant}} - \theta_{\text{PWP}}^{\text{plant}}}{\theta_{\text{MSW}}^{\text{plant}} - \theta_{\text{PWP}}^{\text{plant}}}, & \theta_{\text{PWP}}^{\text{plant}} \leq \theta_W^{\text{plant}} \leq \theta_{\text{MSW}}^{\text{plant}} \\ 1, & \theta_{\text{MSW}}^{\text{plant}} \leq \theta_W^{\text{plant}} \end{cases} $$

(26)

where the factor $R_W$ (unitless) increases from 0 to 1 (Fig. 6, Granier et al. 1999).

Figure 6: Illustration of the reduction factor $R_W$ as a function of available soil water content.
If soil water content is below the permanent wilting point, the factor $R_W$ is set to zero. If available soil water resources are above the minimal soil water content $\theta_{MSW}^{plant}$ [V%], the factor $R_W$ is set to one:

$$\theta_{MSW}^{plant} = \theta_{PWP}^{plant} + 0.4 \cdot (\theta_{FC}^{plant} - \theta_{PWP}^{plant})$$ \hspace{1cm} (27)

If the soil water content is between the permanent wilting point and the minimal soil water content, soil water uptake is linearly reduced by the factor $R_W$. The actual water uptake $\theta_{uptake}$ [l/d] of an individual plant is calculated as follows:

$$\theta_{uptake} = R_W \cdot \theta_{demand}$$ \hspace{1cm} (28)

For simplicity, roots are assumed to be (vertical) distributed equally among the soil layers (of the plant’s rooting zone). Soil water uptake of an individual plant ($\theta_{uptake}$) from a single soil layer is then calculated as:

$$\theta_{uptake}^{j} = \frac{\theta_{uptake}}{s_{max}}$$ \hspace{1cm} (29)

where $\theta_{uptake}^{j}$ [l/d/layer] denotes the individual's water uptake from soil layer $j$.

Similarly, gross primary productivity of a plant $GPP_{pot}$ [g ODM/d] is reduced according to the limitation factor $R_W$:

$$GPP_{W} = R_T \cdot GPP_{pot} \cdot R_W$$ \hspace{1cm} (30)

while $GPP_{W}$ [g ODM/d] is the reduced gross productivity of a plant due to water stress ($R_W$) and air temperature effects ($R_T$, see also section 3.7).

Total soil water uptake (or transpiration) of all plants on a patch can further be restricted by potential evapotranspiration ($PET$ in [mm/d]) and permanent wilting point (entire soil). If the sum of transpiration of all plants (sum of $\theta_{uptake}$ for all plants on a patch in [mm/d], with $1 \text{ lH}_2\text{O/m}^2 = 1 \text{ mmH}_2\text{O}$) and interception of rainfall by plants on a patch ($RI$ in [mm/d]) exceeds the $PET$, then transpiration (or total soil water uptake $\theta_{uptake}^{patch} = \sum_{all \text{ plants on patch}} \theta_{uptake}$ in [mm/d]) and gross productivity ($GPP_{W}$) of all plants is reduced proportionally by the factor (unitless):
\[ f_{PET} = \frac{PET - RI}{\sum_{all\ plants} \theta_{uptake}} \]  \hspace{1cm} (31)

Interception \( RI [\text{mm/d}] \) of rainfall by plants (before rainfall is percolating into the soil) is thereby calculated in the CENTURY soil model as follows:

\[ RI = \left( 0.0003 \cdot B_{litter}^{\text{surface}} + 0.0006 \cdot \sum_{all\ plants} B_{\text{shoot}}^{\text{on\ patch}} \right) \cdot 0.8 \]  \hspace{1cm} (32)

where \( B_{litter}^{\text{surface}} [\text{g ODM/patch}] \) is the patch’s surface litter pool and \( B_{\text{shoot}} [\text{g ODM}] \) is the plants’ aboveground biomass.

Further, if total soil water uptake (of all plants) would result in a soil water content (\( \theta_{soil}^W \) of the entire soil) below the permanent wilting point (\( \theta_{PW}^W \) of the entire soil), then total soil water uptake (or transpiration \( \theta_{uptake}^{patch} \)) and gross productivity (\( GPP^W \)) of all plants is reduced by the factor (unitless):

\[ f_{PW} = \frac{\theta_{soil}^W - \theta_{PW}^W}{\sum_{all\ plants} \theta_{uptake}} \]  \hspace{1cm} (33)

3.9 Nitrogen competition

3.9.1 Nitrogen non-fixing species

Nitrogen uptake of a plant is determined dependent on the nitrogen content of the soil (\( N_{soil} \) in [g/m²]), the individual’s ability to access nitrogen resources (\( N_{access} \) in [g/m²/d]) and its nitrogen demand (\( N_{demand} \) in [g/m²/d]).

To calculate \( N_{demand} \) [g/m²/d] (here, mainly from the mineral nitrogen pool of nitrate \( \text{NO}_3N \)), we calculate the amount of nitrogen required for growth of new leaves, new root branches and for seed production. For this, we calculate a preliminary net productivity \( NPP_{pot} \) (see section 3.11, based on \( GPP^W \) already constrained by soil water conditions and air temperature) and divide its carbon content by pre-defined \( CN \) ratios (of green and brown plant material).

\[ N_{demand} = alloc_{\text{shoot}} \cdot \frac{f_c \cdot NPP_{pot}}{CN_{\text{green}}} + (alloc_{\text{root}} + alloc_{\text{rep}}) \cdot \frac{f_c \cdot NPP_{pot}}{CN_{\text{brown}}} \]  \hspace{1cm} (34)
where $alloc_x$ are allocation rates to different carbon pools of a plant ($x = \text{shoot, root and reproduction}$). $CN_{\text{green}}$ and $CN_{\text{root}}$ are constant species-specific ratios of carbon to nitrogen contents in the respective pools and $f_C$ denotes the fraction of carbon in organic dry matter (here, we use $f_C = 0.43$).

Before plants use the available soil nitrogen, we assume that their demands can be partly fulfilled by nitrogen relocated within the plant from leaves which turn from green to senescent (section 3.14). If demands cannot be fulfilled by relocated nitrogen from senescent leaves, the remaining demand is covered by soil nitrogen resources (for which plants have to compete with each other).

The amount of soil nitrogen $N_{\text{access}}$ which is potentially available for use by an individual plant is calculated by:

$$N_{\text{access}} = \sum_{j<s_{\text{max}}} F_j \cdot N_j$$  \hspace{1cm} (35)

where $N_{\text{access}}$ [g/m²/d] denotes the available nitrogen in soil to which the plant has access and $F_j$ represents a root competition factor. The factor $F_j$ regulates the amount of nitrogen an individual can access by competing with other individuals. $F_j$ is defined as the percentage of root branch lengths of the plant in relation to total root branch length (of all plants per soil layer $j$):

$$F_j = \frac{\left( \frac{\text{length}_{\text{root}}}{s_{\text{max}}} \right)_{j < s_{\text{max}}} \sum_{\text{all plants}} \left( \frac{\text{length}_{\text{root}}}{s_{\text{max}}} \right)_{j < s_{\text{max}}} \text{on patch with } j < s_{\text{max}}}{\sum_{\text{all plants}} \left( \frac{\text{length}_{\text{root}}}{s_{\text{max}}} \right)_{j < s_{\text{max}}} \text{on patch with } j < s_{\text{max}}}$$  \hspace{1cm} (36)

We assume that the plant’s total root branches $\text{length}_{\text{root}}$ are distributed equally among the soil layers (in its rooting zone, Fig. 5). The potential nitrogen uptake $N_{\text{uptake}}$ [g/m²/d] is then defined as:

$$N_{\text{uptake}} = \min(N_{\text{demand}}, N_{\text{access}})$$  \hspace{1cm} (37)

Net production of a plant can be reduced due to limitation in available soil nitrogen (see section 3.11). Therefore, we introduce a limitation factor $R_N$ which is calculated by:
\[ R_N = \frac{N_{\text{uptake}}}{N_{\text{demand}}} = \min\left(1, \frac{N_{\text{access}}}{N_{\text{demand}}} \right) \] (38)

3.9.2 Nitrogen fixing species

Symbiotic nitrogen fixation, e.g. by legumes, is modeled using the following assumptions:

- N-fixing species never compete for nitrogen with other plants. Thus, the limitation factor \( R_N \) always equals one.
- Plants loose carbon for uptake of nitrogen via symbiosis. A specific fraction \( \text{rhiz}_\% \) of net primary production \( NPP \) is therefore provided to rhizobia which is not available anymore for structural growth or recruitment.

In GRASSMIND positive effects of nitrogen-fixing species occur as those species do not take part in the nitrogen competition process and thus, more nitrogen resources in soil are available for N-non-fixing plants. Further, all species contribute to soil nitrogen via decomposition after plant death.

3.10 Respiration

We consider respiratory costs for maintenance of structural tissue (shoot and root biomass) and for growth of plants. Maintenance costs \( r_{\text{main}} \) [g ODM/d] are assumed to be proportional to the green shoot biomass \( B_{\text{shoot}}^{\text{green}} \) and living root biomass \( B_{\text{root}} \):

\[ r_{\text{main}} = r_m \cdot f_T \cdot \left( B_{\text{shoot}}^{\text{green}} + B_{\text{root}} \right) \] (39)

where \( r_m \) is a constant maintenance respiration rate [1/d] and the factor \( f_T \) accounts for changing demands for maintenance respiration with varying air temperature (see section 3.7). Growth respiratory costs are modeled by a constant parameter \( r_g \) (unitless).

3.11 Net primary production

A plant’s gross primary production is used for (a) respiratory costs, (b) growth of an individual’s shoot and root and (c) reproduction. Losses due to respiration (maintenance and growth) lead to the individual’s net primary production \( NPP_{\text{act}} \) [g ODM/d]:

\[ \text{\( NPP_{act} = R_N \cdot (1 - r_g) \cdot (GPP_{act} - r_{main}) \)} \] (39)

where \( GPP_{act} \) [\( \text{gODM/d} \)] is the actual gross primary production which can be reduced according to environmental limitations or competition (derived from the potential \( GPP_{pot} \)):

\[ GPP_{act} = f_{PET} \cdot f_{PWP} \cdot R_W \cdot R_T \cdot GPP_{pot} \] (40)

where \( R_W, f_{PET}, f_{PWP}, R_N, \) and \( R_T \) (all ranging in \([0,1]\)) account for reductions due to soil water limitations (\( R_W, f_{PET}, f_{PWP}, \) equations 26, 31 and 33), soil nitrogen limitation (\( R_N, \) equation 38), and temperature effects (\( R_T, \) equation 22), respectively.

### 3.13 Allocation of net primary production

Net primary production \( NPP_{act} \) (equation 39) is allocated to (a) shoot biomass, (b) root biomass and (c) to reproduction as follows:

- the fraction allocated to the shoot (\( alloc_{shoot} \)) is a species-specific parameter
- the fraction allocated to the root (\( alloc_{root} \)) is derived from the fixed species-specific shoot-root ratio \( sr \) (equation 4)

\[ alloc_{root} = \frac{alloc_{shoot}}{sr} \] (41)

- the remaining fraction is allocated to the reproduction pool

\[ alloc_{rep} = 1 - alloc_{shoot} - alloc_{root} \] (42)

For seedlings, the fraction allocated to the reproduction pool is zero (when plant age is below \( age_{rep} \)). Hence, the fraction allocated to the shoot is adjusted as follows:

\[ alloc_{shoot} = \frac{sr}{sr + 1} \] (43)

### 3.14 Growth of a plant
Allocation of produced biomass (dependent on the allocation fractions, section 3.13) and senescence (dependent on leaf life span LLS and root life span RLS, section 3.3.1) result in the following changes in the plant's biomass pools:

\[
\frac{\Delta B_{\text{sen}}}{\Delta t} = \frac{1}{\text{LLS}} \cdot B_{\text{green}}^{\text{shoot}}
\]

\[
\frac{\Delta B_{\text{green}}}{\Delta t} = \text{alloc}_{\text{shoot}} \cdot NPP_{\text{act}} - \frac{1}{\text{LLS}} \cdot B_{\text{green}}^{\text{shoot}}
\]

\[
\frac{\Delta B_{\text{root}}}{\Delta t} = \text{alloc}_{\text{root}} \cdot NPP_{\text{act}} - \frac{1}{\text{RLS}} \cdot B_{\text{root}}
\]

\[
\frac{\Delta B_{\text{rep}}}{\Delta t} = \text{alloc}_{\text{rep}} \cdot NPP_{\text{act}}
\]

Based on the change in the biomass pools \(B_{\text{shoot}}\) and \(B_{\text{root}}\), the new biomass values for the different pools are calculated and the geometrical variables of an individual plant are updated.

With regard to a plant’s biomass pools, the respective nitrogen pools are updated dependent on the species-specific CN ratios (of green and brown plant material) and a biomass-to-carbon conversion factor \((f_C = 0.43)\). For those shoot biomass parts, which turn from green to senescent ones (equation 44), leaf nitrogen is relocated and used for nitrogen demands in the subsequent time step (section 3.9.1):

\[
N_{\text{relocated}} = \frac{1}{\text{LLS}} \cdot B_{\text{green}}^{\text{shoot}} \cdot f_C \cdot \left(\frac{1}{CN_{\text{green}}} - \frac{1}{CN_{\text{brown}}}\right)
\]

3.15 Management

Management of grasslands is included in GRASSMIND in terms of mowing, irrigation and fertilization. All three events are characterized by the following information:

- dates of management events (i.e. frequency)
- intensity (e.g. cutting height, fertilizer amount, amount of water supply)

In terms of mowing, the height of all plants on a patch greater than the cutting height (e.g. 10 cm) is decreased, thus leading to a modified parameter \(h_w_{\text{modified}}\). For the following time steps, increment in aboveground biomass only contributes to height growth until the time step at which the original parameter \(h_w\) is reached again.

Fertilizer and water supply by irrigation contribute to soil resources in the upper soil layer.
References


